

## Experiment Name: Kirchhoffs\_Laws

# Overview



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## Fundamental Concepts in Electrical Engineering Lab2 - Kirchhoff's Voltage and Current Laws

### Objectives

- Learn Kirchhoff's Voltage Law
- Learn Kirchhoff's Current Law
- Apply Kirchhoff's Voltage Law to the analysis of a series circuit
- Apply Kirchhoff's Current Law to the analysis of a parallel circuit

### Components

- Resistors: 1Ohm (1%, 0.25W) 3 pieces, 100Ohms (10%, 0.5W), 560Ohms(10%,0.5W), 820Ohms(10%, 0.5W)
- Circuit prototyping breadboard
- Electric wires

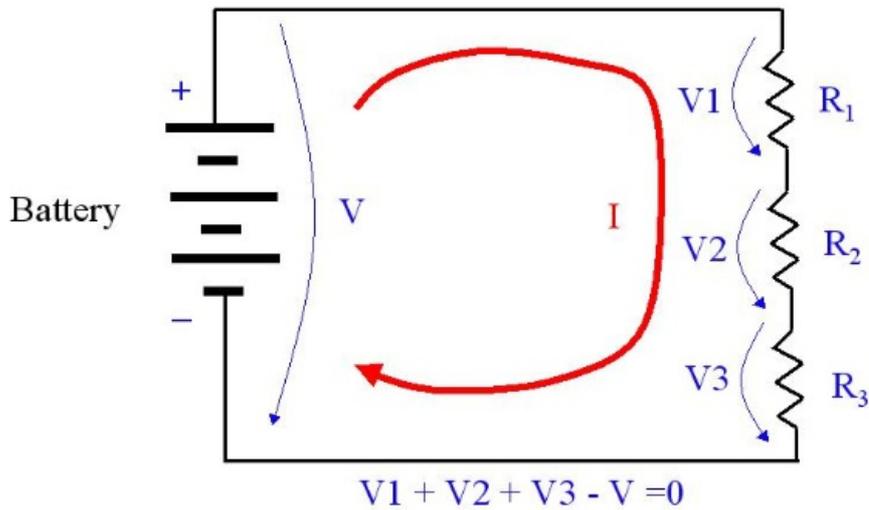
### Equipment

- Adjustable power supply (at least 0 - 5V voltage range, and 0.5A maximum current)
- Tektronix TBS 1202B-EDU Oscilloscope

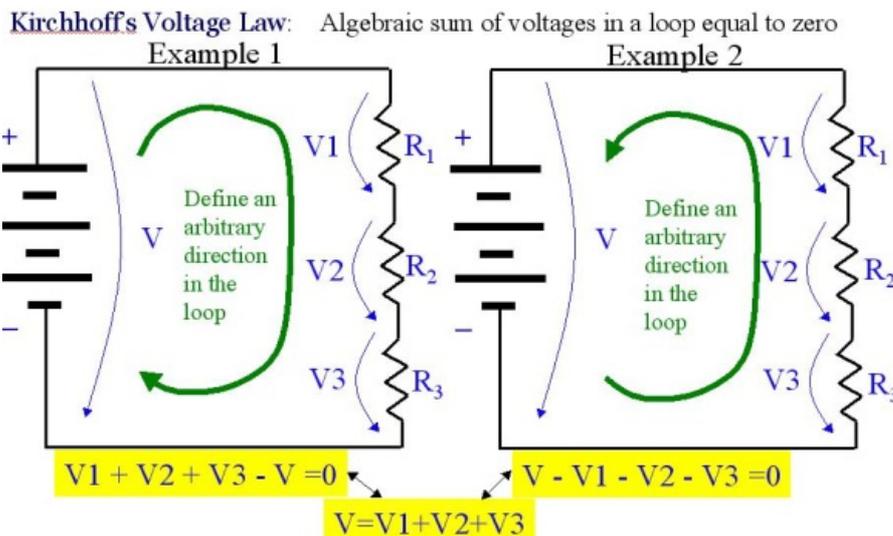
## Theory

### 1. Kirchhoff's Voltage Law

Kirchhoff's voltage law describes the relationship between the voltage sources and voltage drops on loads in a circuit loop. A simple example is shown in the following figure. According to Kirchhoff's voltage law the algebraic sum of voltages in a loop is equal to zero. Notice the polarities of voltages on the battery and the three resistors. In red it is shown the direction of electric current as flowing from the positive terminal of the battery through the three resistors and back into the battery. The voltage on the battery has polarity opposite to the direction of electric current and therefore it is algebraically added as negative value.



In the example above we knew the direction of electric current; however, there are often cases when we do not know the direction of electric current through the circuit loop. To apply Kirchhoff's voltage law we don't really need to know the actual direction of electric current; we can just define an arbitrary direction and write Kirchhoff's voltage law for that direction. This is exemplified in the figure below:

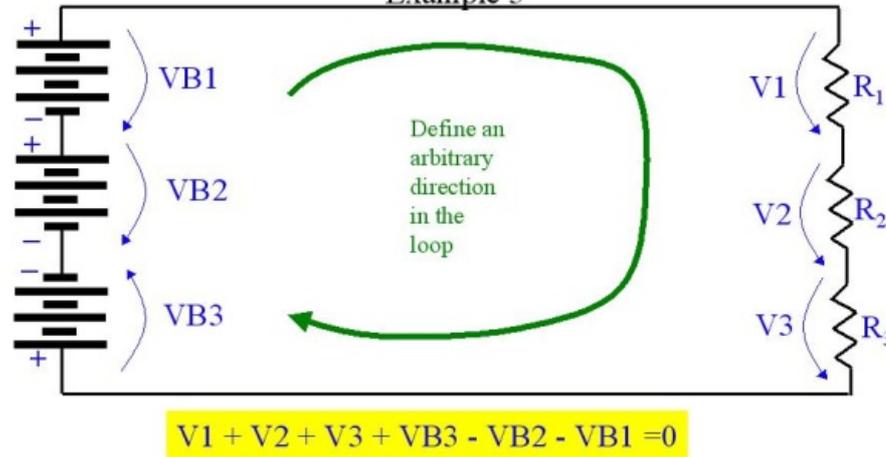


In this example we defined an arbitrary direction through the loop, clockwise in the example 1 and counter-clockwise in example 2. Notice that the Kirchhoff's voltage laws written for these two opposite arbitrary directions result in the same equation.

To further clarify the Kirchhoff's voltage law let's look at the following example, which includes multiple voltage sources and connected with reverse polarities.

**Kirchhoff's Voltage Law:** Algebraic sum of voltages in a loop equal to zero

**Example 3**



So depending on the arbitrary direction chosen, some supply voltages are summed with a positive sign and others with a negative sign.

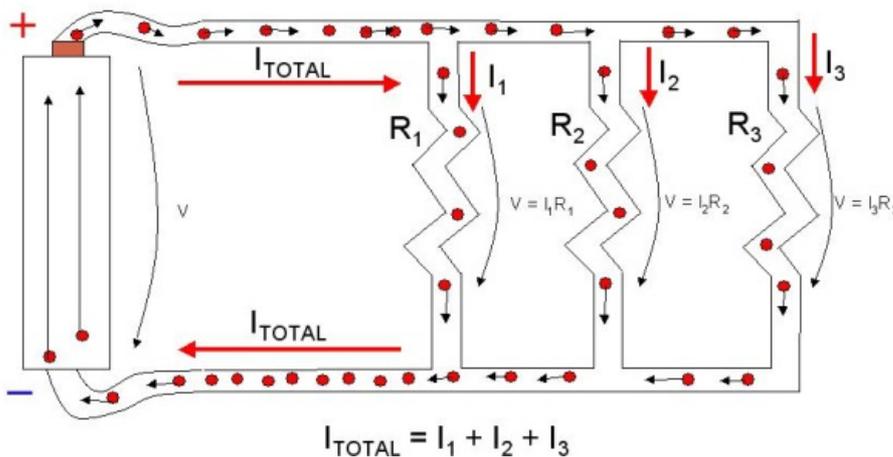
**2. Kirchhoff's Current Law**

Kirchhoff's current law describes quantitatively the relationship between the intensity of electric currents that flow in and out of a circuit node. From an intuitive perspective, by looking at the figure below we can deduce that as  $I_{total}$  current splits into three currents,  $I_1$ ,  $I_2$ , and  $I_3$ , the number of charges of  $I_{total}$  that flow through the wire in a unit of time would have to split among the three paths of  $I_1$ ,  $I_2$ , and  $I_3$ . So if we combine the number of charges that flow in one second in  $I_1$ ,  $I_2$ , and  $I_3$  currents the sum should be equal to  $I_{total}$ 's number of charges that flow in one second (no charges are lost and no charges are created). This is exactly what Kirchhoff's current law states, that:

$$I_{total} = I_1 + I_2 + I_3,$$

or in the general form: the algebraic sum of electric currents flowing into a circuit node is equal to zero.

**Resistors Connected in Parallel**

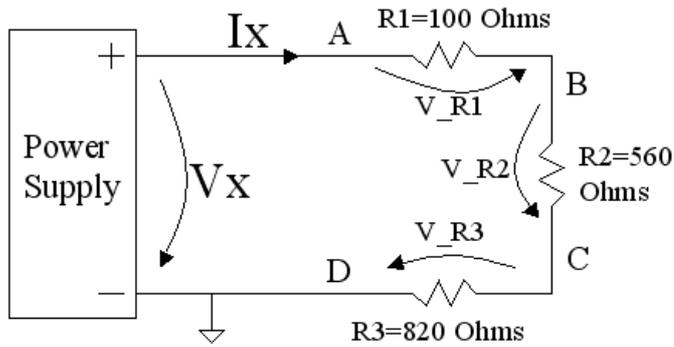


How does the current split? How much would it go through one resistor and how much through the others? Let's look at an example:  $R_1 = 1k\Omega$ ,  $R_2 = 3k\Omega$  and  $R_3 = 9k\Omega$ , all connected in parallel to a 9V voltage supply. Applying Ohm's law to each resistor,  $V = I_1 * R_1$ ,  $V = I_2 * R_2$ , and  $V = I_3 * R_3$ , we know V and  $R_1$ ,  $R_2$ ,  $R_3$ , so we can calculate the value of each current:  $I_1 = 9mA$ ,  $I_2 = 3mA$ , and  $I_3 = 1mA$ .

**Experimental Setup**

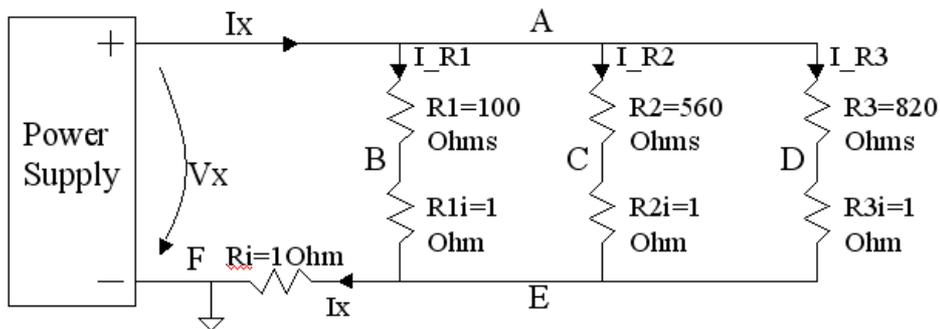
**Part 1: Kirchhoff's Voltage Law**

Construct the circuit shown in the diagram below and continue with the steps listed in the "Procedure" section.



### Part 2: Kirchhoff's Current Law

Construct the circuit shown in the diagram below and continue with the corresponding steps listed in the "Procedure" section.



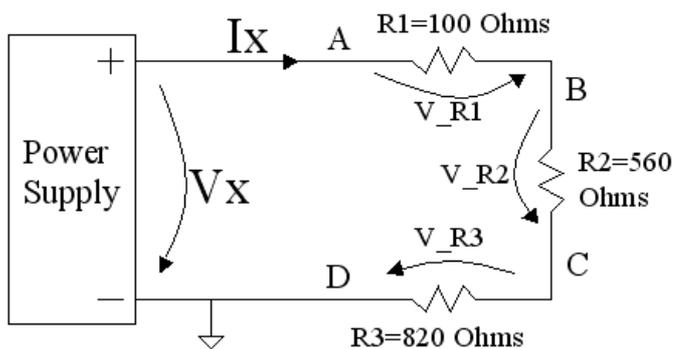
In this circuit the  $1\text{ Ohm}$  1% resistor is used as a current to voltage converter with the transfer function:  $1\text{ A} \rightarrow 1\text{ V}$ ,  $100\text{ mA} \rightarrow 100\text{ mV}$ ,  $10\text{ mA} \rightarrow 10\text{ mV}$ ,... This way we can use one channel of the oscilloscope to probe the current through the circuit.

## Experiment Name: Kirchhoffs\_Laws

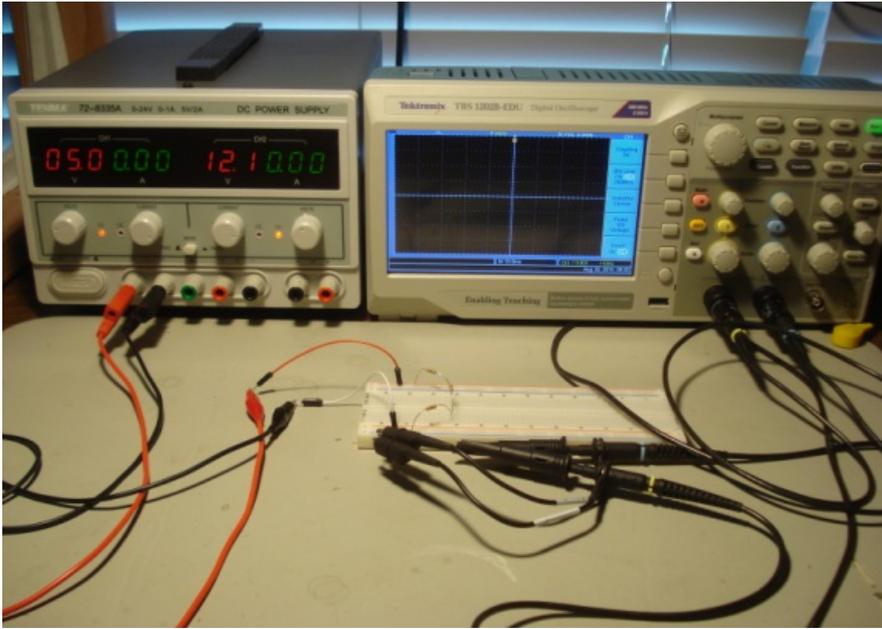
### Procedure

#### Step 1

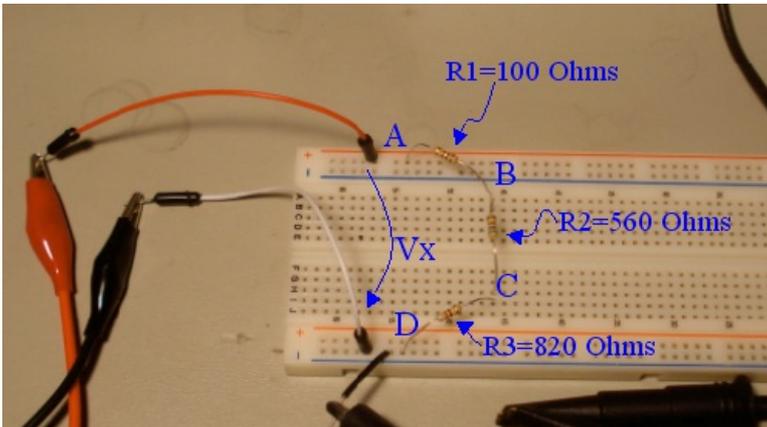
Construct the series circuit in the diagram below and connect it to the power supply.



Here is an example of testbench setup:

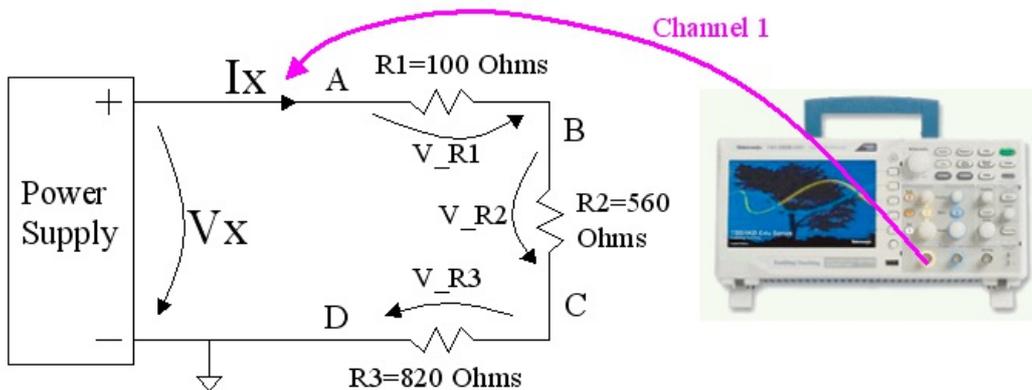


And here is a more detailed picture of the circuit:



## Step 2

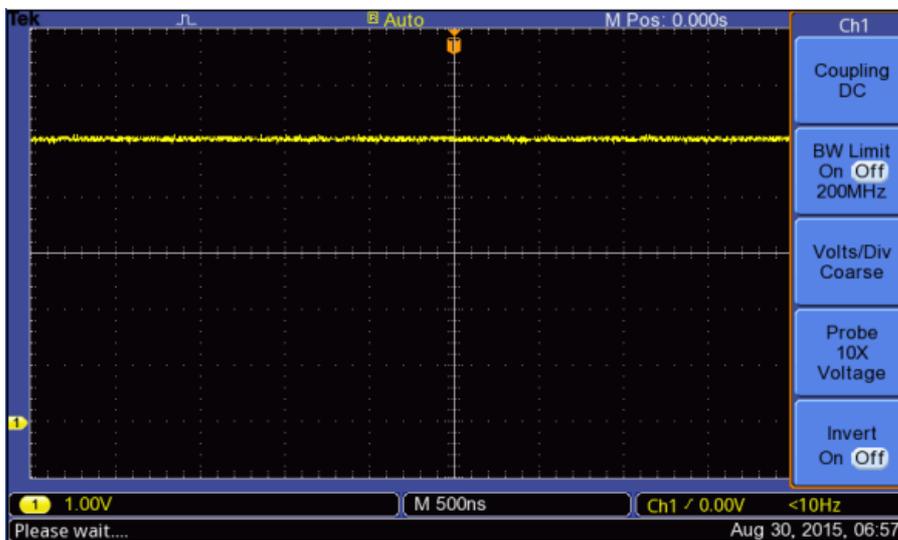
- Connect Channel 1 of the TBS1000B-EDU oscilloscope to node A (the ground clip of the probe will be connected to the ground node "D" of the circuit).



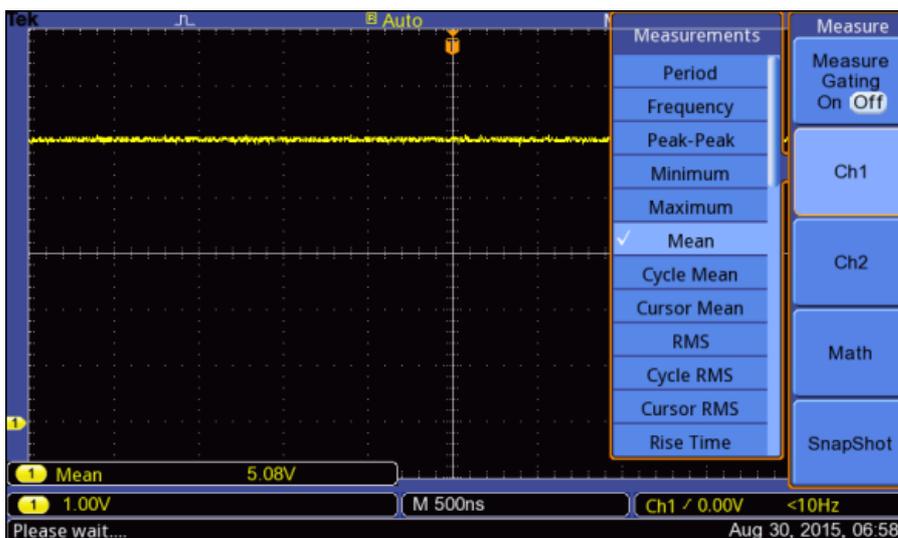
- Setup the power supply voltage to 5V.
- Setup the Oscilloscope Channel 1 Input to DC mode, Vertical scale = 1V/div, and Channel 2 input to DC mode, Vertical scale = 1V/div.

- Setup the Oscilloscope time base to 500ns/div (this is not important here since we measure DC voltages that do not change in time and are represented as horizontal lines on the display)
- Setup the Oscilloscope Trigger to Auto mode.
- Alternately press the "Autoset" button and make the adjustments to settings after the oscilloscope displays the waveforms.

With this setup Channel 1 measures the voltage  $V_x$ , as shown in the screenshot below:



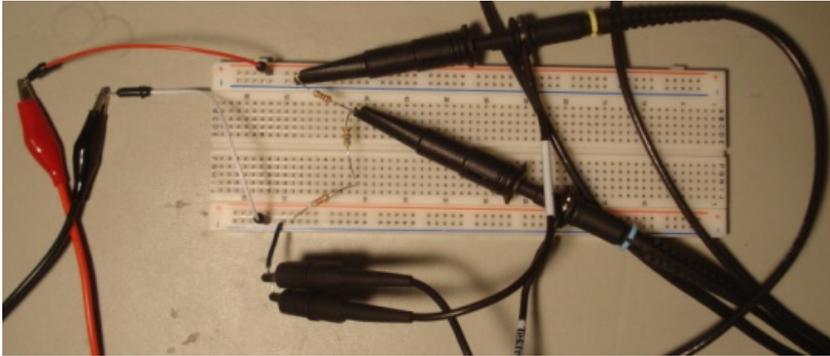
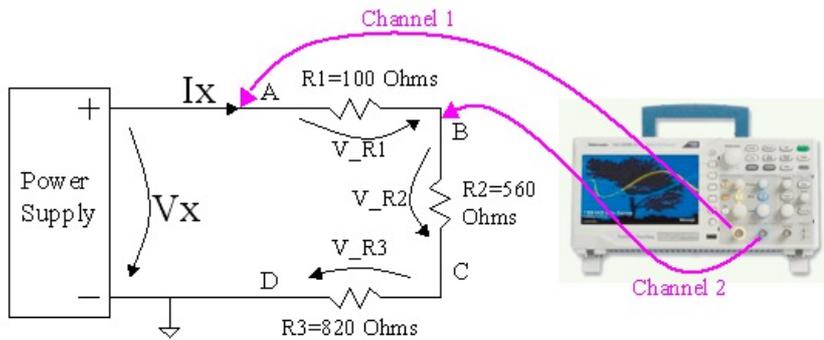
- Use the built-in "Measure" function of the oscilloscope to measure the voltage level of channel 1. Select "Mean" from the measure menu, like it is shown in the picture below:



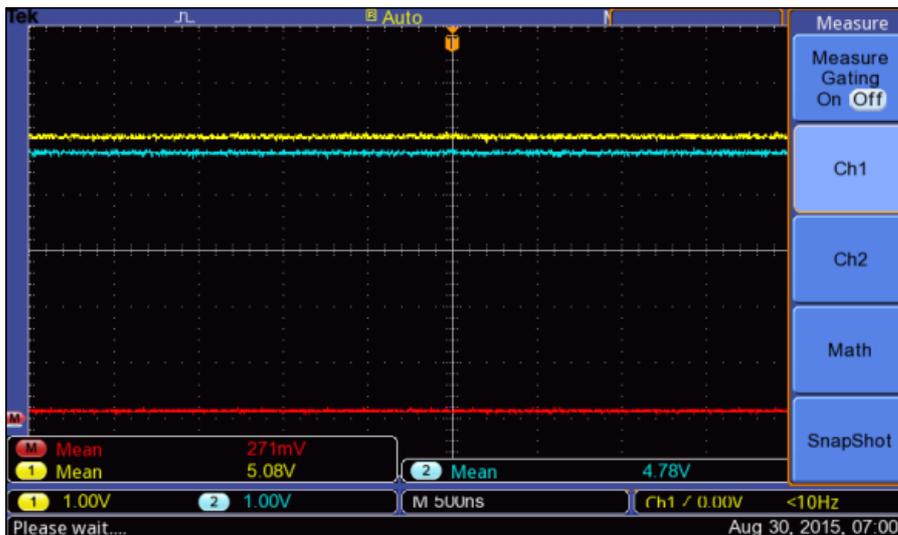
- The measured value represents the voltage  $V_x$  in the circuit schematic. Record this value since we will use it in Step 6 below.
- Insert a screenshot of your measurement in this step of the lab.

## Step 3

- Connect Channel1 to node A and Channel2 to node B of the circuit. The ground clips are connected to the ground node of the circuit (Node D). Here is a picture of this setup on the schematic on the testbench:



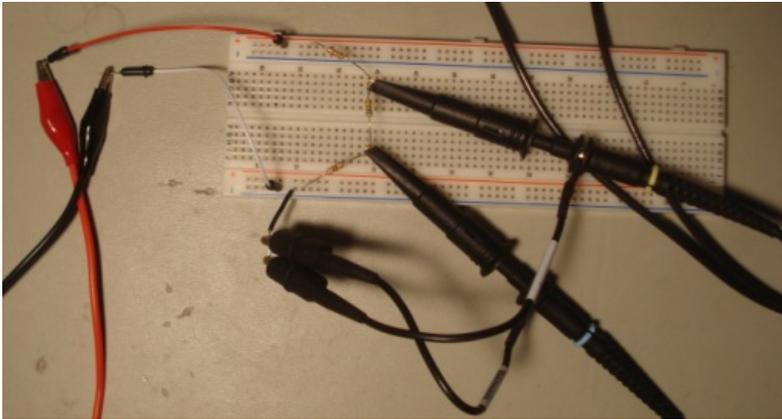
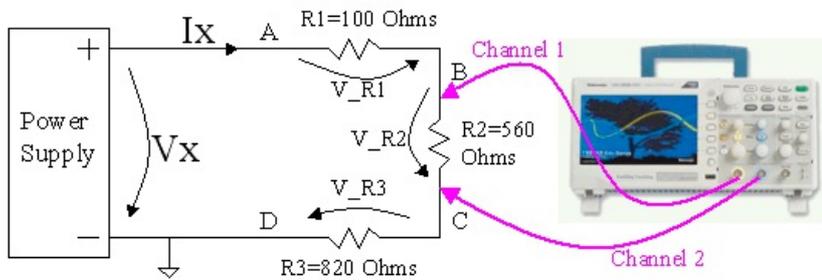
- In this picture Channel1 is the yellow marked probe and Channel2 is the blue marked probe. Set the "Math" built-in function of TBS1202B-EDU oscilloscope to display Channel1-Channel2. Align the zero Volts levels of Channel1, Channel2, and Math traces, and set the built-in measure function to display the "Mean" value of each trace, as shown in the picture below:



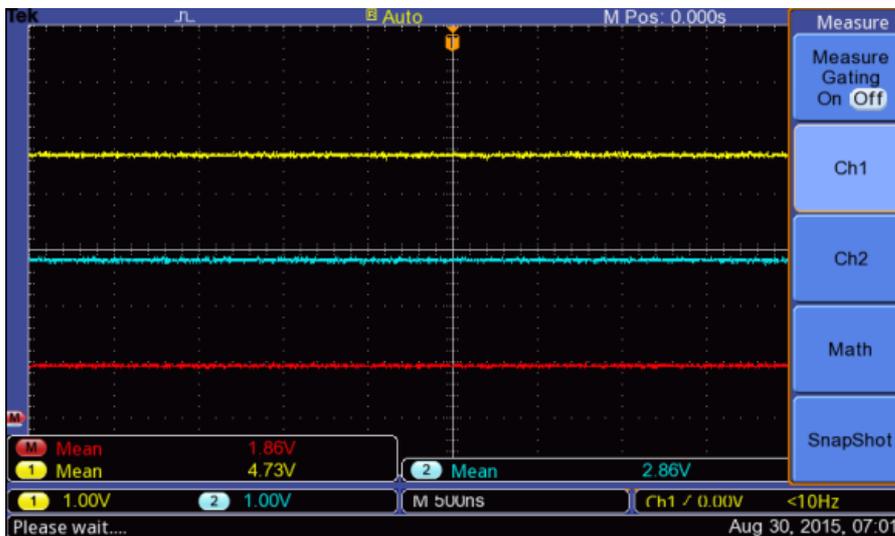
- The measured value of the Math trace represents the voltage drop on R1 resistor. Record this value since we will use it in Step 6 below.
- Insert a screenshot of the oscilloscope display in this step.

## Step 4

- Connect Channel1 to node B and Channel2 to node C of the circuit. The ground clips are connected to the ground node of the circuit (Node D). Here is a picture of this setup on the schematic and on the testbench:



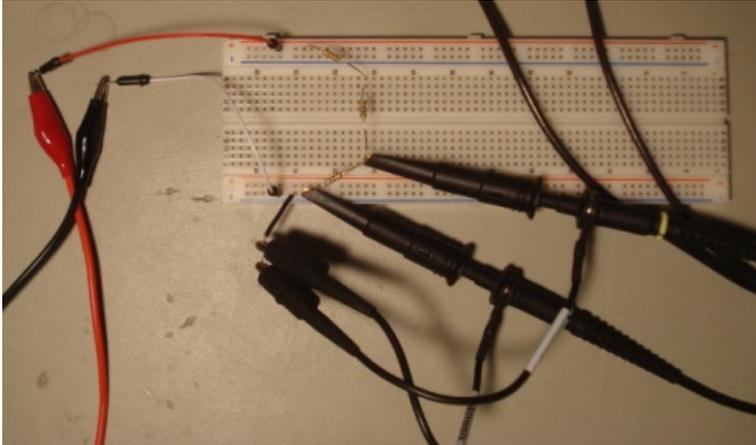
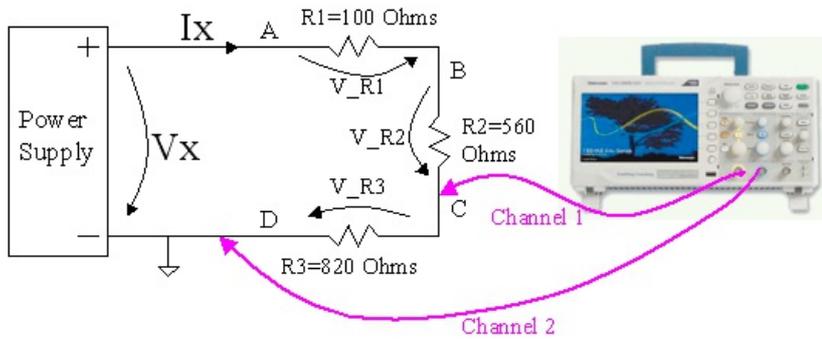
- In this picture Channel1 is the yellow marked probe and Channel2 is the blue marked probe. Set the "Math" built-in function of TBS1202B-EDU oscilloscope to display Channel1-Channel2. Align the zero Volts levels of Channel1, Channel2, and Math traces, and set the built-in measure function to display the "Mean" value of each trace, as shown in the picture below:



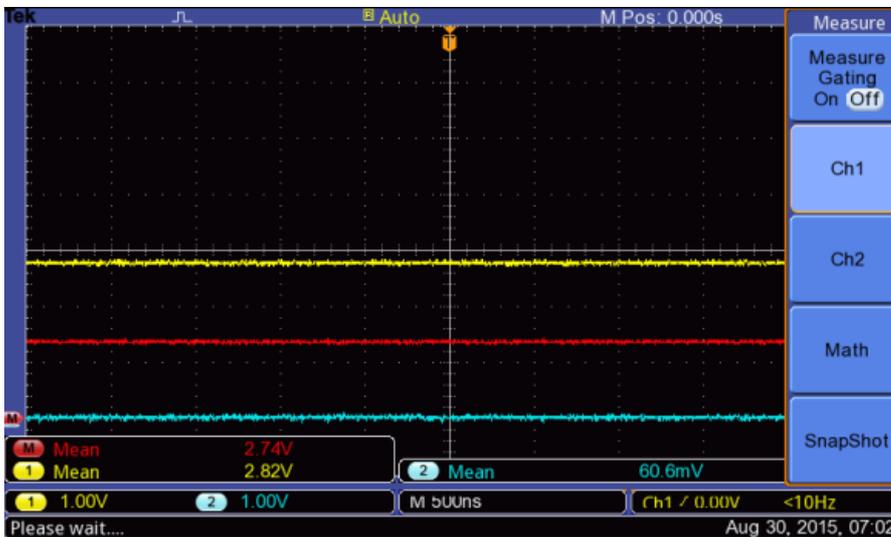
- The measured value of the Math trace represents the voltage drop on R2 resistor. Record this value since we will use it in Step 6 below.
- Insert a screenshot of the oscilloscope display in this step.

## Step 5

- Connect Channel1 to node C and Channel2 to node D of the circuit. The ground clips are connected to the ground node of the circuit (Node D). Here is a picture of this setup on the schematic and on the testbench:



- In this picture Channel1 is the yellow marked probe and Channel2 is the blue marked probe. Set the "Math" built-in function of TBS1202B-EDU oscilloscope to display Channel1-Channel2. Align the zero Volts levels of Channel1, Channel2, and Math traces, and set the built-in measure function to display the "Mean" value of each trace, as shown in the picture below:



- The measured value of the Math trace represents the voltage drop on R3 resistor. Record this value since we will use it in Step 6 below.
- Insert a screenshot of the oscilloscope display in this step.

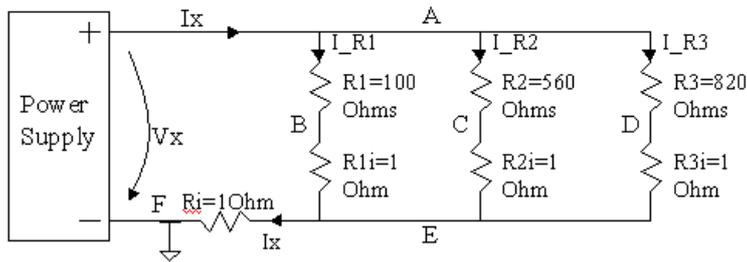
## Step 6

- Calculate the sum of the voltages on R1, R2, and R3 resistors, measured in Steps 3,4, and 5.
- Compare this result with the measured voltage  $V_x$  in Step 2. Is voltage  $V_x$  equal to the sum  $V_{R1} +$

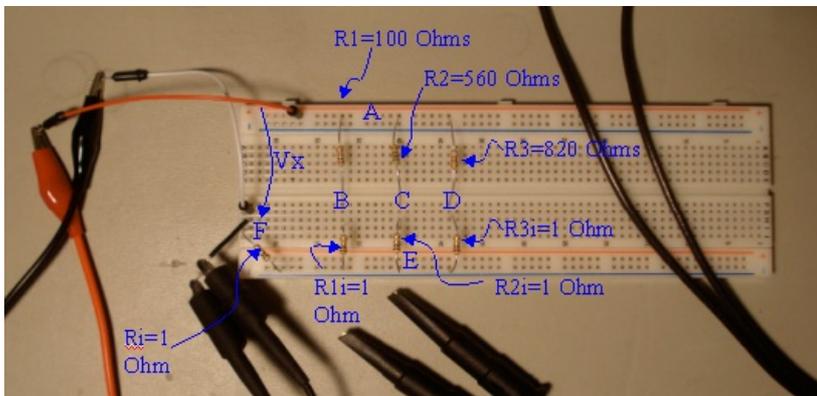
- $V_{R2} + V_{R3}$ ?
- Did we prove Kirchhoff's voltage law? Explain your answer.

## Step 7

Construct the parallel circuit in the diagram below and connect it to the power supply.

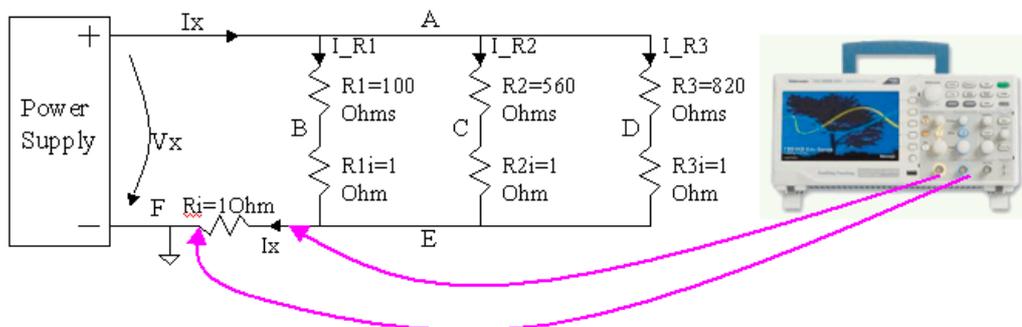


Here is a more detailed picture of the circuit:

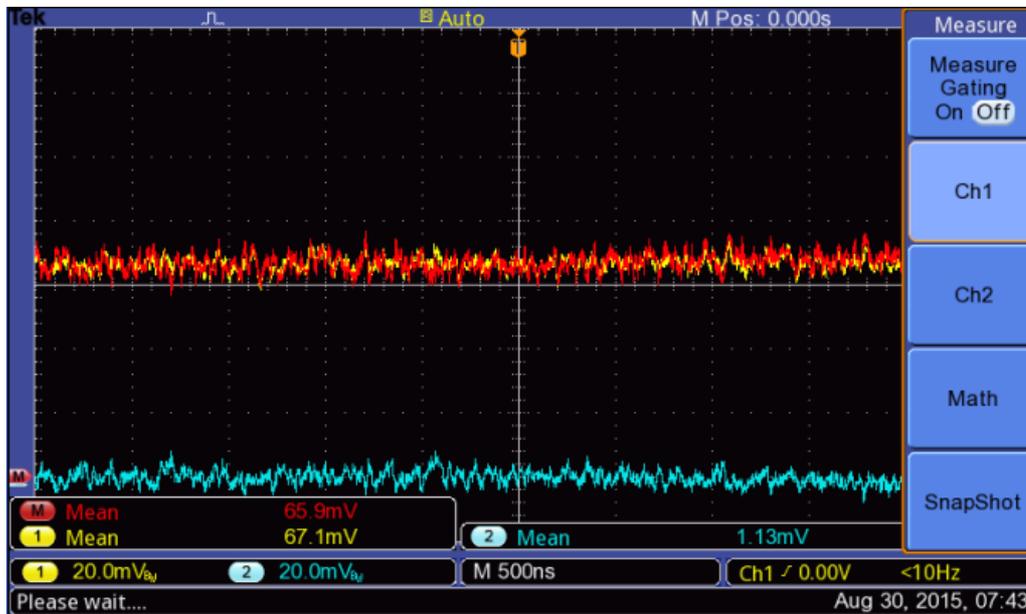


## Step 8

- Setup the power supply voltage to 5V.
- Setup the Oscilloscope Channel 1 Input to DC mode, Vertical scale = 20mV/div, and Channel 2 input to DC mode, Vertical scale = 20mV/div.
- Setup the Oscilloscope time base to 500ns/div (this is not important here since we measure DC voltages that do not change in time and are represented as horizontal lines on the display)
- Setup the Oscilloscope Trigger to Auto mode.
- Alternately press the "Autoset" button and make the adjustments to settings after the oscilloscope displays the waveforms.
- Connect Channel 1 to node E and Channel 2 to node F of the circuit, as shown in the diagram below:



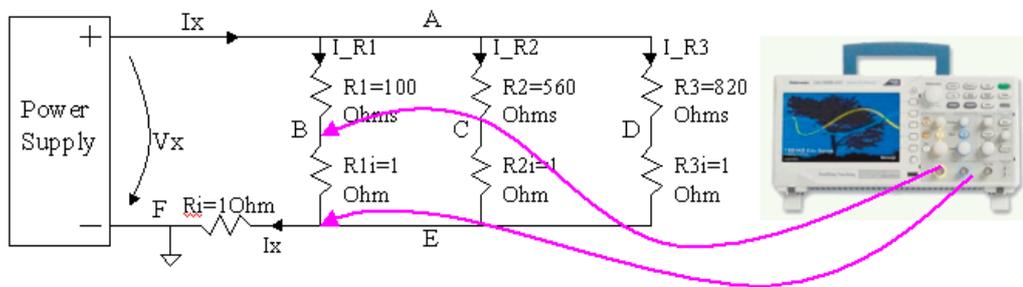
- Setup the Math built-in function of the oscilloscope to calculate and display Channel 1 - Channel 2 trace.
- With this setup the oscilloscope screen should display three horizontal lines representing the voltages at nodes E, F, and their difference.
- Use the built-in "Measure" function of the oscilloscope to measure the voltage levels of the channel 1, channel 2, and "Math" traces. Select "Mean" from the measure menu, like it is shown in the picture below:



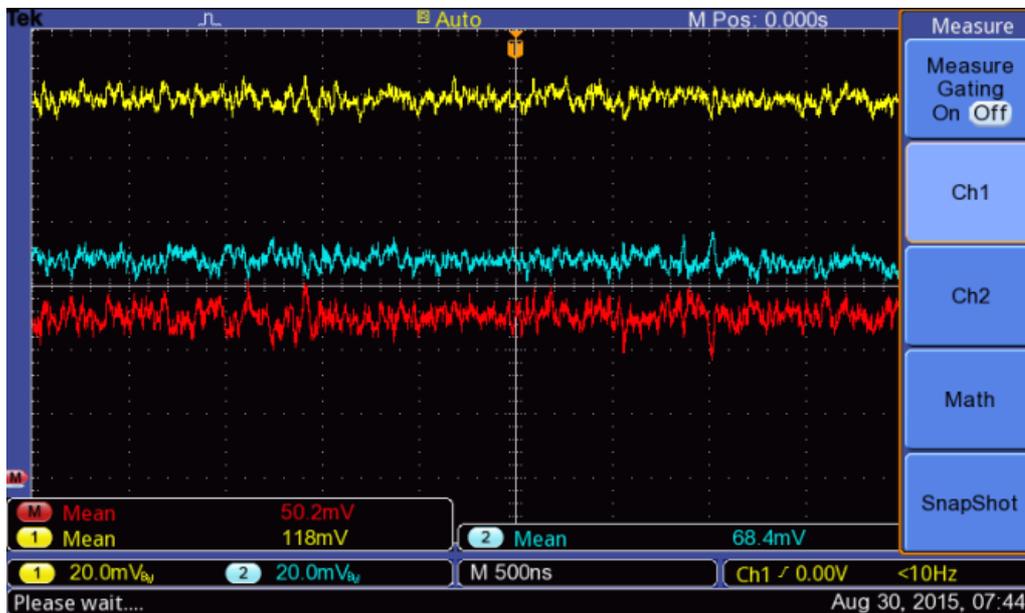
- These "Math" trace represents the voltage drop on  $R_i=1\text{ Ohms}$ , and using Ohm's law we can translate this quantity into the current flowing through  $R_i$  by using a 1:1 conversion factor. In the waveform example above  $V_{Ri}=65.9\text{mV}$  which translates into  $65.9\text{mA}$  flowing through  $R_i$  resistor. This current is equal to  $I_x$  in the schematic diagram.
- Insert a screenshot of the oscilloscope display showing channel 1, channel 2, Math signals, and the measured values.
- Determine  $I_x$  from the voltage measured for "Math" trace. Record this value since we will use it in Step 12 below.

## Step 9

- Connect Channel 1 to node B and Channel 2 to node E of the circuit, as shown in the diagram below:



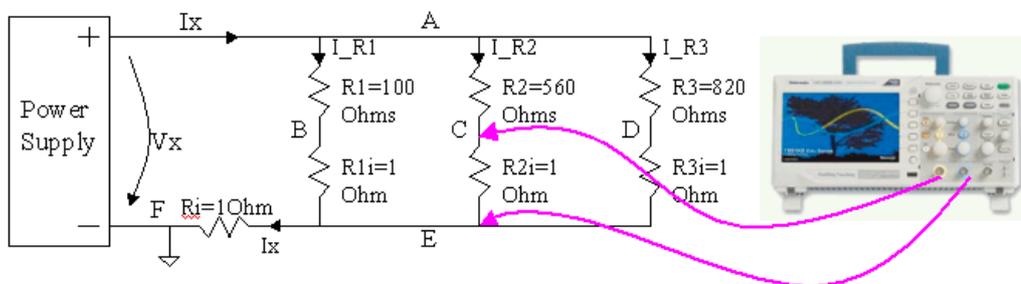
- Setup the Math built-in function of the oscilloscope to calculate and display Channel 1 - Channel 2 trace.
- With this setup the oscilloscope screen should display three horizontal lines representing the voltages at nodes B, E, and their difference.
- Use the built-in "Measure" function of the oscilloscope to measure the voltage levels of the channel 1, channel 2, and "Math" traces. Select "Mean" from the measure menu, like it is shown in the picture below:



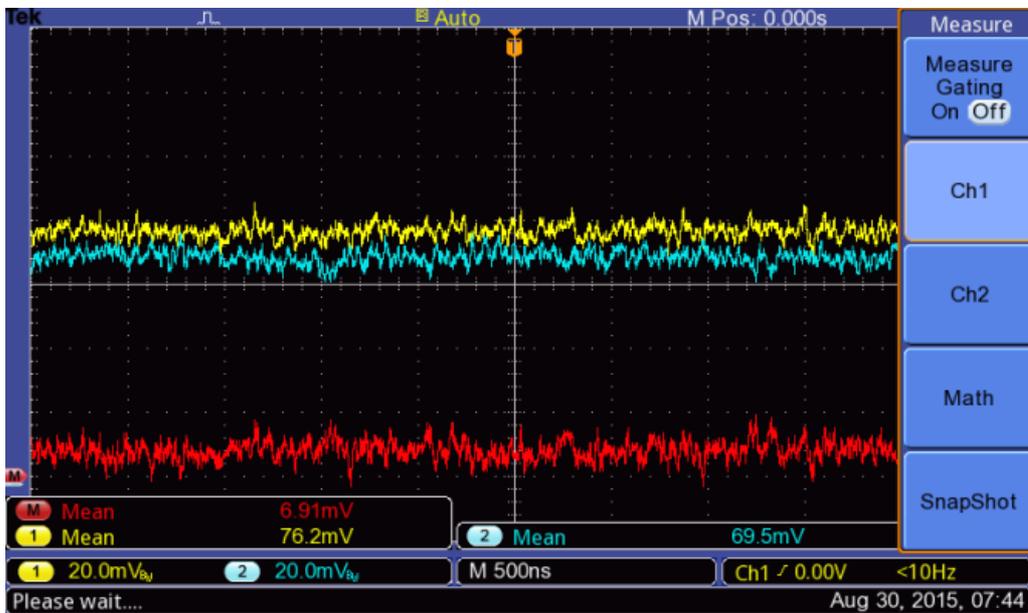
- These "Math" trace represents the voltage drop on  $R1i=1\text{Ohms}$ , and using Ohm's law we can translate this quantity into the current flowing through  $R1i$  by using a 1:1 conversion factor. In the waveform example above  $V_{Ri}=50.2\text{mV}$  which translates into  $50.2\text{mA}$  flowing through  $R1i$  resistor. This current is equal to  $I_{R1}$  in the schematic diagram.
- Insert a screenshot of the oscilloscope display showing channel 1, channel 2, Math signals, and the measured values.
- Determine  $I_{R1}$  from the voltage measured for "Math" trace. Record this value since we will use it in Step 12 below.

## Step 10

- Connect Channel 1 to node C and Channel 2 to node E of the circuit, as shown in the diagram below:



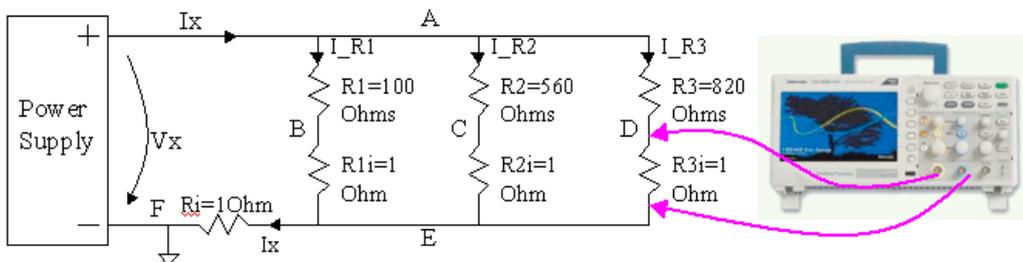
- Setup the Math built-in function of the oscilloscope to calculate and display Channel 1 - Channel 2 trace.
- With this setup the oscilloscope screen should display three horizontal lines representing the voltages at nodes C, E, and their difference.
- Use the built-in "Measure" function of the oscilloscope to measure the voltage levels of the channel 1, channel 2, and "Math" traces. Select "Mean" from the measure menu, like it is shown in the picture below:



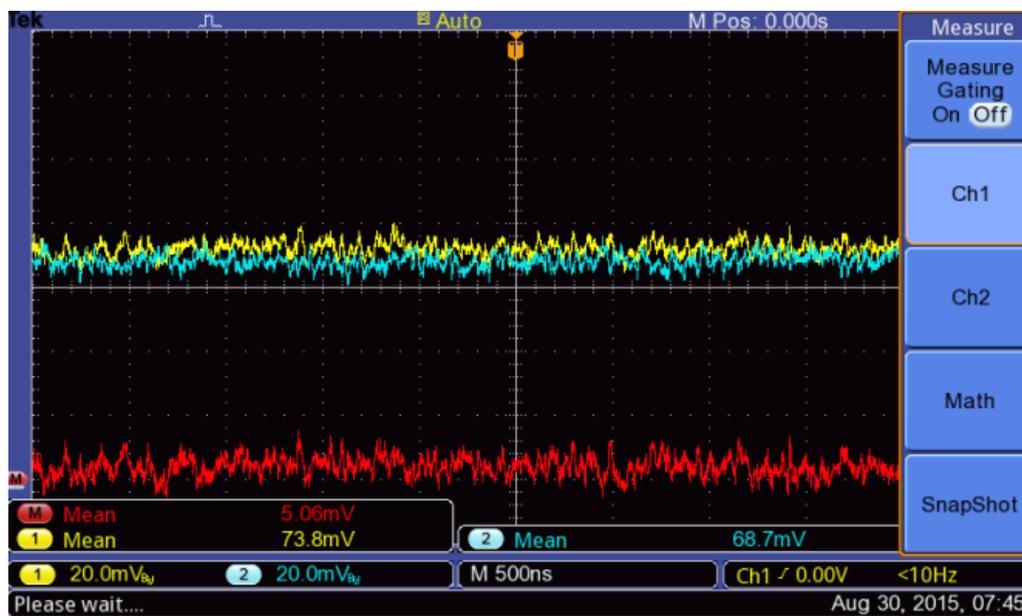
- These "Math" trace represents the voltage drop on  $R_{2i}=1\text{Ohms}$ , and using Ohm's law we can translate this quantity into the current flowing through  $R_{2i}$  by using a 1:1 conversion factor. In the waveform example above  $V_{R_{2i}}=6.91\text{mV}$  which translates into  $6.91\text{mA}$  flowing through  $R_{2i}$  resistor. This current is equal to  $I_{R2}$  in the schematic diagram.
- Insert a screenshot of the oscilloscope display showing channel 1, channel 2, Math signals, and the measured values.
- Determine  $I_{R2}$  from the voltage measured for "Math" trace. Record this value since we will use it in Step 12 below.

## Step 11

- Connect Channel 1 to node D and Channel 2 to node E of the circuit, as shown in the diagram below:



- Setup the Math built-in function of the oscilloscope to calculate and display Channel 1 - Channel 2 trace.
- With this setup the oscilloscope screen should display three horizontal lines representing the voltages at nodes D, E, and their difference.
- Use the built-in "Measure" function of the oscilloscope to measure the voltage levels of the channel 1, channel 2, and "Math" traces. Select "Mean" from the measure menu, like it is shown in the picture below:



- These "Math" trace represents the voltage drop on  $R_{3i}=1\text{Ohms}$ , and using Ohm's law we can translate this quantity into the current flowing through  $R_{3i}$  by using a 1:1 conversion factor. In the waveform example above  $V_{R_{3i}}=5.06\text{mV}$  which translates into  $5.06\text{mA}$  flowing through  $R_{3i}$  resistor. This current is equal to  $I_{R3}$  in the schematic diagram.
- Insert a screenshot of the oscilloscope display showing channel 1, channel 2, Math signals, and the measured values.
- Determine  $I_{R3}$  from the voltage measured for "Math" trace. Record this value since we will use it in Step 12 below.

## Step 12

- Calculate the sum of the currents through  $R_1$ ,  $R_2$ , and  $R_3$  resistors, measured in Steps 9,10, and 11.
- Compare this result with the measured current  $I_x$  in Step 8. Is the current  $I_x$  equal to the sum  $I_{R1} + I_{R2} + I_{R3}$ ?
- Did we prove Kirchhoff's current law? Explain your answer.